

MATH 101A: ALGEBRA I
PART C: TENSOR PRODUCT AND MULTILINEAR
ALGEBRA

This is the title page for the notes on tensor products and multilinear algebra.

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