

MATH 101A: ALGEBRA I
PART D: GALOIS THEORY

This is the title page for the notes on Galois Theory.

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