

Below you will find the list of some of the topics which may appear on the exam, and some suggestions for preparation. References are made to the corresponding pages/statements in the textbook.

1. Review the homework assignments 1–8 and the two quizzes.
2. Know the definitions of
 - (a) basic operations with sets (union, intersection, complement, containment and equality of sets, Cartesian product, power set)
 - (b) a function, injective, surjective, and bijective functions, composition of functions, inverse of a function, a graph of a function, inverse images and level sets
 - (c) bounded subsets of \mathbf{R} and bounded real-valued functions, increasing/decreasing real-valued functions
 - (d) logical operations and quantifiers (\forall , \exists , \neg , \wedge , \vee , \Leftarrow , \Leftrightarrow)
 - (e) finite, infinite, countable sets, the size of a finite set, two sets having the same cardinality
3. Be familiar with the following:
 - (a) the arithmetic-geometric mean inequality, the triangle inequality (4–5)
 - (b) properties of the real number system (16–17; you do not have to remember which properties are axioms and which are propositions)
 - (c) direct, contrapositive and “by contradiction” proof techniques (35–39)
 - (d) principles of induction (51–57) and strong induction (63–64), well-ordering property of \mathbf{N} and the method of descent (64–66)
 - (e) the fact that two finite sets have the same number of elements (size) if and only if there exists a bijection between them
 - (f) the fact that if two functions are injective/surjective/bijective, then so is their composition (Proposition 4.30, proved in class)
 - (g) that two finite sets have the same number of elements (size) if and only if there exists a bijection between them (Proposition 4.37, proved in class)
 - (h) examples of countable sets discussed in Chapter 4 and in class (89–90)